Econ 302, Summer 2011

Final practice

There are four parts, each worth 25 points. There are five bonus questions worth a total of 10 points, but they cannot raise your score above 100/100.

Part I: Market structure
Part II: Market interventions

Part III: Consumer theory and production

Part IV: Short answer

Bonus

In this practice, you will find all possible topics for Parts I-III and some examples for Part IV and Bonus. The specific questions asked in the exam may be different; and scores written next to each problem are rough estimates.

Part I. [25] Market structure

x. [20] <u>Duopoly and collusion</u> – find the payoffs for a high-low game and put them in the game matrix

There are two firms with identical per-unit costs of MC = 40 and no fixed costs.

Demand is given by $P_D = 400 - 3Q$.

a. Find the Cournot equilibrium quantities $q_1^{\ C}$ and $q_2^{\ C}$ and the Cournot equilibrium price P^C .

b. Find the firms' profits in the Cournot equilibrium Π_1^c and Π_2^c .

c. Suppose the firms collude by setting $q_1^m = \frac{1}{2}Q^M$ and $q_2^m = \frac{1}{2}Q^M$. Find these quantities and the price P^m .

d. What are the firms' profits Π_1^m and Π_2^m ?

e. Suppose firm 1 follows the collusive agreement by setting output at half the monopoly output q_1^m , but firm 2 breaks the agreement by setting output at the Cournot level q_2^c . What is the price $P^{m,c}$ that results?

f. What are the firms' profits Π_1 and Π_2 in the case described in part e?

g. Enter the payoffs into a normal-form game matrix and circle the unique Nash Equilibrium outcome.

h. Draw the extensive-form game if firm 1 moves first, and circle the unique Subgame-Perfect Nash Equilibrium.

x. [15] (WB16#1) Monopoly from production – deriving C(q), choosing L^* , K^* , optimal P^M and Q^M , CS, PS, DWL, LI, ϵ

A monopolist has production technology given by

$$F(L, K) = L^{1/2}K^{1/2}$$

$$MP_L = \frac{1}{2} K^{1/2} / L^{1/2}$$

$$MP_K = \frac{1}{2} L^{1/2}/K^{1/2}$$

Demand is given by P = 66 - 3Q and input prices are w = 9 for labor and r = 4 for capital.

a. Find the monopolist's cost function.

b.	Find the monopolist's optimal quantity and price Q^M and P^M .
C.	How much labor and capital L^M and K^M will the monopolist buy to produce Q^M ?
d.	What is the Dead Weight Loss of this monopoly?
о. С	Timat is the Bead Weight 2000 of this monopoly.

e. What is the Lerner Index? What is the elasticity of Demand at Q^M?

x. [20] (WB19#3) Cournot duopoly vs monopoly – Cournot equilibrium q_1^c , q_2^c and P^c ; CS, PS, DWL, LI, ϵ

Market (inverse) Demand is $P_D=200-5Q$ and the two duopolists have constant marginal costs $MC_1=50$ and $MC_2=50$ and no fixed costs.

a. Find each firm's revenues, expressed as functions of their output choices q_1 and q_2 .

b. Find the (Cournot) equilibrium P^{c} , q_1^{c} and q_2^{c} .

c. Find the Lerner Index in the Cournot Equilibrium.

d. Find what the outcome would be if the firms behaved competitively P^* and Q^* .

e. What is the Dead Weight Loss of the duopoly? What are the Consumer Surplus and Producer Surplus?

f. Find the market price and quantity if the firms merged into a monopoly P^{M} and Q^{M} .

g. What would be the Dead Weight Loss of the monopoly? Also find the Consumer Surplus and Producer Surplus.

x. [10] Stackelberg vs Cournot duopoly – Cournot equilibrium, Stackelberg equilibrium q_1^s , q_2^s and P^s , compare profits

Two firms have identical marginal costs MC = 20 and no fixed costs. Demand is given by $P_D = 200 - 3Q$

a. Find the Stackelberg equilibrium when firm 1 chooses output first, q_1^s , q_2^s and P^s .

b. Find the firms' profits in the Stackelberg equilibrium.

c. Find the Cournot equilibrium when the firms choose output at the same time, $q_1^{\ c}$, $q_2^{\ c}$ and P^c .

d. Find the firms' profits in the Cournot equilibrium.

x. [10] Monopoly – optimal P^M and Q^M , CS, PS, DWL, LI, ϵ

A monopolist has marginal cost MC = 2Q and no fixed costs. Demand is given by $P_{\text{D}} = 200 - 3\text{Q}$

a. Find the monopolist's optimal quantity and price Q^M and P^M .

- b. What is the monopolist's marginal cost at Q^M?
- c. Find what the outcome would be if the monopolist behaved competitively P^* and Q^* .

d. Graph Demand and Marginal Cost curves.

e. Find the Consumer Surplus, Producer Surplus and Dead Weight Loss under the monopoly.

x. [5] Perfect competition

Competitive firms have identical costs, $C = 75 + 3q^2$, with marginal costs MC = 6q. Market (inverse) Demand is given by Q = 150 - P.

a. Find the firms' break-even price.

b. Graph the Supply and Demand curves.

c. Find the equilibrium P* and Q*.

d. Calculate the Consumer Surplus.

x. [5] Market power

a. What does it mean for a firm to have market power?

b. In imperfectly competitive markets, when consumers are *more elastic*, do producers have more or less market power? Explain.

Part II. [25] Market interventions

x. [15] <u>Price restrictions from inverse Supply and Demand</u> – effectiveness, shortage/surplus, CS, PS, DWL

The US government is going to set a price floor of $P^F = 400 . (Inverse) Demand and Supply are

$$P_D = 300 + 2I - 4Q$$

$$P_S = 100 + Q$$

and income is I = 150.

- a. Find the equilibrium *before the price floor* is used, P* and Q*.
- b. How much is traded *after the price floor* is used?
- d. Make a Supply and Demand graph, indicating the Consumer Surplus, Producer Surplus and Dead Weight Loss *after the price floor*.

e.	find an expression for the Demand curve, which gives the quantity demanded as a function of income I and the price P.
f.	Before the price floor, is the good a necessity, a luxury or inferior?
g.	After the price floor, is the good a necessity, a luxury or inferior?
h.	Do consumers or producers benefit from the price floor, or neither? (You may need to

compute the CS and PS both before and after the price floor)

x. [15] <u>Per-unit tax from inverse Supply and Demand</u> – graphing, CS, PS, DWL, G, elasticities, incidence

A per-unit tax of T = \$40 is going to be used in a market with (inverse) Demand and Supply curves given by...

$$P_D = 300 - 7Q$$

$$P_S = 100 + Q$$

a. Find the competitive equilibrium **before the tax** P^* and Q^* .

- b. After the tax, how much is...
 - ... traded?
 - ...paid by consumers?
 - ...paid to suppliers?

c. Find the Producer Surplus, Consumer Surplus, Government Revenue and Dead Weight Loss *after the tax*.

x. [10] (not on the test, but good practice) Market intervention for policy

The Demand and Supply for cigarettes are given by

 $Q_D = 9000/P \text{ and}$

 $Q_s = 10P$

where quantities are measured in millions of packs of cigarettes each week. The government wants to reduce consumption to Q = 10 million packs.

a. What price ceiling could the government set to reduce consumption to Q = 10?

b. What price floor could the government set to reduce consumption to Q = 10?

c. What per-unit tax could the government charge to suppliers to reduce consumption to Q = 10?

d. Consumers and producers are both worse off after the tax. Can the government fully compensate them with the revenues it collects? Explain.

x. [5] <u>Price restrictions</u> – shortage, surplus

The Demand and Supply for soap are given by

 $Q_D = 200 - 5P$ and

 $Q_S = 5P$

a. Find the equilibrium.

- b. Find a price floor that causes a surplus.
- c. How large is the surplus for the price floor you chose?
- d. At a price floor below the equilibrium price, is there a shortage or a surplus?

Part III. [25] Consumer theory and production.

x. [∞] <u>Income and Substitution Effects and Giffen goods</u>

If consumption of pasta falls when the price of pasta falls, ...

- (A) ... it must be that pasta is a "bad."
- (B) ... it must be that all other goods are necessities.
- (C) ... it must be that consumption of pasta falls when income rises.
- (D) ... it must be that the Income Effect for pasta is weak.

x. [10] Consumer choice for Cobb-Douglas preferences

The consumer faces prices P_X = 10 and P_Y = 2, and has income I = 500 and preferences given by

$$U = X^3 Y^2$$

$$MU_X = 3X^2Y^2$$

$$MU_Y = 2X^3Y$$

a. Graph the consumer's budget set, labeling axes and intercepts.

d. Find the consumer's optimal bundle X^* and Y^* and mark it on your graph.

x. [10] Price decomposition

A consumer has income I = 600 to spend on goods X and Y. The price of Y is P_Y = 4. The price of X is initially P_X = 100, but it later decreases to P_X ' = 25.

$$U = X^{1/2}Y^{1/2}$$

$$MU_X = \frac{1}{2} Y^{1/2} / X^{1/2}$$

$$MU_Y = \frac{1}{2} X^{1/2} / Y^{1/2}$$

a. How much does the consumer choose X^* and Y^* when $P_X = 10$?

b.	How much does the consumer choose X^{**} at the new price $P_{X}' = 25$?
c.	How much money, M, would the consumer need to have to be just as well off after the price change?
d.	How much of the change in the consumer's choice is due to the Income Effect?

Is X normal or inferior? Explain by defining each term.

d.

x. [5] <u>Deriving Demand for Cobb-Douglas preferences.</u>

A consumer's utility function is $U = X^2Y$ with marginal utilities MUx = 2XY and $MUy = X^2$. The consumer has \$300 to spend. Derive expressions for the consumer's Demand for X and Y in terms of the prices P_X and P_Y .

x. [5] Consumer choice with perfect substitutes preferences

A consumer's utility function is U = X+2Y with $MU_X = 1$ and $MU_Y = 2$.

- a. True or False? These are perfect-complements preferences.
- b. The prices are $P_X = 1$ and $P_Y = 3$. Derive expressions for the consumer's Demand for X and Y in terms of the consumer's income I.

x. [5] <u>Consumer choice with perfect complements preferences</u>

A consumer has preferences described by $U = min\{2X, Y\}$ and income I = 95. Market prices are $P_X = 5$, $P_Y = 7$.

a. Graph three of the consumer's indifference curves.

b. How much will the consumer buy of X and Y?

x. [5] <u>Budgets</u> – graphing, identifying the MRT, whether or not a bundle is affordable, how much is bought when \$z is spent

A consumer has I = 180 to spend on X any Y. The prices are P_X = 4 and P_Y = 3.

a. Graph the consumer's budget set, labeling axes and intercepts.

- b. If the consumer spends 60 on X and 120 on Y, how much X and Y are bought?
- c. On your graph, mark the bundle found in part b.
- d. Is the bundle X = 20, Y = 20 affordable?
- x. [5] <u>Increasing, decreasing or constant returns-to-scale</u>

A firm's production function is given by $F(L,K) = L^{1/2}K^{3/4}$. Are there increasing, decreasing or constant returns to scale? Show your work.

x. [5] <u>Cobb-Douglas technology</u> – deriving costs

A firm has technology given by

$$F(L, K) = L^{1/2}K^{1/2}$$

$$MP_L = \frac{1}{2} K^{1/2} / L^{1/2}$$

$$MP_K = \frac{1}{2} L^{1/2} / K^{1/2}$$

The prices of inputs are w = 25 for labor and r = 16 for capital.

- a. How do we know that there are Decreasing Marginal Returns to Labor?
- b. Find the firm's cost function.

$$F(L, K) = 3L + 5K, MP_L = 3, MP_K = 5$$

The prices of inputs are w = 25 for labor and r = 16 for capital.

a. Draw the isoquant for q = 150.

b. How much L and K should the firm purchase to produce q = 150 units of output?

c. What is the cost of the input bundle that you found in b?

x. [5] <u>Fixed-proportions technology</u> – graphing the isoquant, deriving costs

A firm's technology is described by the production function

 $F(L,K) = \min\{3L,2K\}$

The wage is w = 6 and the rental rate is r = 10.

- a. What kind of technology does the firm have?
- b. Graph the firm's isoquant for q = 30, labeling the axes and important points.

c. Derive the firm's cost function C(q), which gives the cost for any output goal q.

Part IV. [25] Short answer

x. [5] <u>Supply-and-Demand: calculating equilibrium</u> – complement or substitute, normal or inferior, elasticities, find P* and Q*

$$Q_D = 500 - 41 - 3P^G - 6P$$

$$Q_{S} = 100$$

Income is I = 25 and the price of a related good is $P^G = 20$.

a. Find the equilibrium.

b. Find the income elasticity at the equilibrium.

- c. Is the good normal or inferior? Also, is it a luxury, a necessity or neither?
- d. Is the *other good* a complement or a substitute?

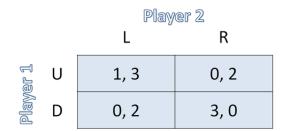
x. [5] <u>Supply-and-Demand basics: perfectly inelastic/elastic Supply/Demand, related goods, two shifts</u>

a. The Supply of tickets to the World Cup finals is *perfectly inelastic*. What happens to the equilibrium price and quantity if a substitute becomes cheaper (for example, if the game is streamed live online for free)? Illustrate your answer with a graph.

Hamburgers and catsup are complements. The price of beef – an input for hamburgers – falls. What happens to the equilibrium price and quantity in the market for catsup?
 Illustrate your answer with one or more graphs.

c. There is an improvement in technology at the same time as a reduction in the number of consumers. What combined effect do these changes have on the equilibrium price and quantity? Explain using one or more graphs.

x. [5] Games: find all NE of a 2x2/normal-form game

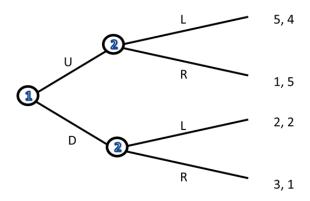


a. Find all Nash Equilibria of the game above.

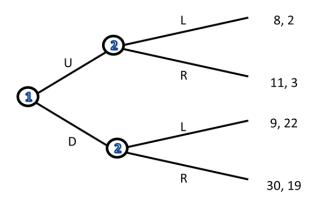
b. Find all Nash Equilibria of the game above.

c. Are any of the pure strategy Nash Equilibria found above inefficient? Which, if any?

x. [5] Games: find the SPNE outcome of an extensive-form game



a. Find the unique Subgame-Perfect Nash Equilibrium outcome of the game above and circle it.



- b. Find the unique Subgame-Perfect Nash Equilibrium outcome of the game above and circle it.
- c. For each of the cases above, is there another outcome that is a Pareto improvement?

x. [5] Edgeworth box/Pure exchange: graphing

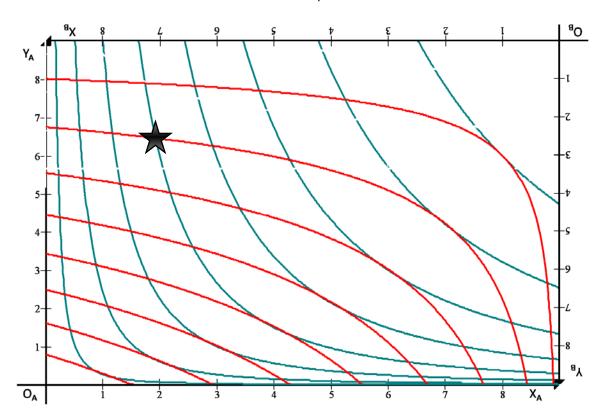
Consumer A has endowment $X_A^0 = 5$ and $Y_A^0 = 10$; and consumer B has endowment $X_B^0 = 7$, $Y_A^0 = 12$.

a. Draw the Edgeworth box, labeling the four axes.

b. Mark the endowment point, labeling the four quantities.

x. [5] Edgeworth box/Pure exchange: concepts

The Edgeworth box for two consumers is given below, along with several of their indifference curves. The endowment point is marked with a star.



- a. Sketch the contract curve, representing all efficient allocations.
- Shade in the allocations that are Pareto improvements on the endowment,
 representing trades the consumers are both willing to make.
- c. Sketch the core, representing the Pareto improvements that are also efficient.

x. [5] Edgeworth box/Pure exchange: equilibrium

Ann and Bob have preferences and endowments given by

a. Find the Marginal Rates of Substitution for each consumer at the endowment allocation, $\mathsf{MRS}_{\mathsf{A}} \text{ and } \mathsf{MRS}_{\mathsf{B}}.$

- b. Is the endowment allocation efficient? Explain.
- c. Find the pure exchange equilibrium price P_X , and quantities X_A^* , Y_A^* , X_B^* and Y_B^* (the price of Y is fixed at $P_Y = 1$).

x. [5] General equilibrium in two markets

Solve for the general equilibrium. Your answer should consist of four numbers: price and quantity for good 1 and good 2.

$$Q_{D1} = 10 - 3P_1 + P_2$$

$$Q_{D2} = 6 - 4P_2 + P_1$$

$$Q_{S1} = -3 + 4P_1$$

$$Q_{S2} = -2 + 6P_2$$

x. [5] (not on test, but good practice) Pareto efficiency

Suppose Ann and Bob have endowments and preferences over goods X and Y given by

$$U_A = XY$$
, $MU_{XA} = Y$, $MU_{YA} = X$ $X_A^0 = 0$, $Y_A^0 = 8$ $U_B = X+Y$, $MU_{XB} = 1$, $MU_{YB} = 1$ $X_B^0 = 10$, $Y_B^0 = 2$

a. State a reallocation of the goods that is a Pareto improvement over the endowment.There is more than one right answer.

b. Show that giving Ann and Bob each 5 units of each good is efficient.

x. [5] Short-run costs and production for Cobb-Douglas

A firm has technology given by

$$F(L, K) = L^{1/3}K^{2/3}$$

$$MP_L = (1/3) K^{2/3}/L^{2/3}$$

$$MP_K = (2/3) L^{1/3}/K^{1/3}$$

The prices of inputs are w = 32 for labor and w = 25 for capital.

Find the firm's short-run cost function if the firm's capital is fixed at K = 4.

Bx. [2] Optimal two-part tariffs

Ann's Demand function for sandwiches from a campus cafeteria is

$$Q_{D} = 20-P$$

The cafeteria has set a price of P = 15 per sandwich, and wants to charge Ann an access fee to get into the cafeteria. What fee P_A should it charge Ann to maximize its revenue?

Bx. [2] Monopoly pricing in two markets – optimal P_1^M , P_1^M , q_1^M and q_2^M .

A monopolist is selling a good it two markets and has marginal cost MC = $2(Q_1 + Q_2)$. (Inverse) Demand in the two markets is given by

$$P_1 = 100 - Q_1$$

$$P_2 = 190 - 3Q_2$$

What prices should the monopolist charge in the two markets to maximize profits?

Bonus. [10]

There will be 5 two-point questions. Some examples of the sort of question you might see...

Bx. [2] Interpreting ICC graphs

Bx. [2] **Define (something)**

- Bx. [2] Show that (something about monopoly and elasticity)
- Bx. [2] Assumptions on preferences, and when they are violated
- Bx. [2] State the two welfare theorems for pure exchange economies
- Bx. [5] <u>Increasing, decreasing or constant returns-to-scale with exotic technology</u>

A firm's production function is given by $F(L,K) = L^{1/2}K^{3/4} + 3K$. Are there increasing, decreasing or constant returns to scale? Show your work.

Bx. [2] Cobb-Douglas technology with non-½ exponents – deriving costs

A firm's technology is given by

$$F(L, K) = L^{2/3}K^{1/3}$$

$$MP_L = (2/3) K^{1/3}/L^{1/3}$$

$$MP_K = (1/3) L^{2/3}/K^{2/3}$$

And the input prices are w = 16, r = 1.

Find the firm's cost function.

Bx. [2] Short-run costs and production for perfect substitutes or fixed-proportions

A firm has a production function F(L, K) = 5L + 4K and a fixed amount K = 10 of capital in the short run. Input prices are w = 2 for labor and r = 5 for capital. Find the firm's short-run cost function.

Bx. [2] <u>Deriving Demand for perfect substitutes or perfect complements preferences</u>

A consumer has a utility function $U = min\{5X, 4Y\}$ and income I = 1000. Find the consumer's demand for X and Y, expressed in terms of the prices of X and Y.

Bx. [2] Exotic budgets

A consumer has income I = 100. The price of good X is $P_X = 5$. The price of good Y is $P_Y = 5$ if the consumer buys fewer than 10 units, but it is lowered to $P_Y' = 2$ for units beyond the first 10 units. Graph the consumer's budget set, labeling any important points.